

## Lorenzo Pettinari: Damping of phonons in Bose gas at low temperature

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Condensed Bose gases can be effectively described in terms of quasi-particles, commonly referred to as  $\textit{phonons}$ . Their dynamics are captured by a  $\textit{c}$ -number condensate Hamiltonian consisting of a quadratic term supplemented by third- and fourth-order perturbative corrections. These additional interaction terms render the phonons unstable, giving rise to two distinct decay processes known as  $\textit{Beliaev}$  and  $\textit{Landau}$  damping. From a mathematical perspective, such decay mechanisms should manifest as a  $\textit{broadening}$  of the Bogoliubov dispersion relation in the thermodynamic limit. To validate this picture, I will present two different approaches to deriving the phonon decay rates. The first is inspired by the  $W^*$ -algebraic framework of Jak\v{s}i\v{c}–Pillet, employing Standard Representations and perturbative expansions of a suitably chosen vector state. The second method is based on the analysis of two-body correlation functions. Both approaches yield the same imaginary correction to the Bogoliubov dispersion relation, which in turn determines the expected broadening. Furthermore, our approaches offer a new perspective on the decay of phonons in terms of the  $\textit{left}$  and  $\textit{right}$  components of these quasi-particles. The talk is based on joint work with Jan Derezi\v{n}ski and may be viewed as a modern elaboration of the classical contributions of Beliaev, Hohenberg–Martin, and others.