Improved mixing for the convex polygon triangulation flip walk

ICALP 2023

Wednesday, July 12, 2023 11:45 AM (20 minutes)

David Eppstein and Daniel Frishberg

Abstract: We prove that the well-studied triangulation flip walk on a convex point set mixes in time $O(n^3 \log^3 n)$, the first progress since McShine and Tetali's $O(n^5 \log n)$ bound in 1997. In the process we give lower and upper bounds of respectively $Omega(1/(sqrt n \log n))$ and O(1/sqrt n)—asymptotically tight up to an $O(\log n)$ factor—for the expansion of the associahedron graph K_n. The upper bound recovers Molloy, Reed, and Steiger's $Omega(n^{3/2})$ bound on the mixing time of the walk. To obtain these results, we introduce a framework consisting of a set of sufficient conditions under which a given Markov chain mixes rapidly. This framework is a purely combinatorial analogue that in some circumstances gives better results than the projection-restriction technique of Jerrum, Son, Tetali, and Vigoda. In particular, in addition to the result for triangulations, we show quasipolynomial mixing for the k-angulation flip walk on a convex point set, for fixed k >= 4.

Presenter: FRISHBERG, Daniel Session Classification: Track A-3