

# Robust Communication Complexity of Matching: EDCS Achieves 5/6 Approximation

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**Abstract:** We study the robust communication complexity of maximum matching. Edges of an arbitrary  $n$ -vertex graph  $G$  are randomly partitioned between Alice and Bob independently and uniformly. Alice has to send a single message to Bob such that Bob can find an (approximate) maximum matching of the whole graph  $G$ . We specifically study the best approximation ratio achievable via protocols where Alice communicates only  $O(n)$  bits to Bob.

There has been a growing interest on the robust communication model due to its connections to the random-order streaming model. An algorithm of Assadi and Behnezhad [ICALP'21] implies a  $(2/3 + \epsilon_0 \sim .667)$ -approximation for a small constant  $0 < \epsilon_0 < 10^{-18}$ , which remains the best-known approximation for general graphs. For bipartite graphs, Assadi and Behnezhad [Random'21] improved the approximation to .716 albeit with a computationally inefficient (i.e., exponential time) protocol.

In this paper, we study a natural and efficient protocol implied by a random-order streaming algorithm of Bernstein [ICALP'20] which is based on edge-degree constrained subgraphs (EDCS) [Bernstein and Stein; ICALP'15]. The result of Bernstein immediately implies that this protocol achieves an (almost)  $(2/3 \sim .666)$ -approximation in the robust communication model. We present a new analysis, proving that it achieves a much better (almost)  $(5/6 \sim .833)$ -approximation. This significantly improves previous approximations both for general and bipartite graphs. We also prove that our analysis of Bernstein's protocol is tight.

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