Robust Communication Complexity of Matching: EDCS Achieves 5/6 Approximation

Wednesday, July 12, 2023 11:45 AM (20 minutes)

Amir Azarmehr and Soheil Behnezhad

Abstract: We study the robust communication complexity of maximum matching. Edges of an arbitrary n-vertex graph G are randomly partitioned between Alice and Bob independently and uniformly. Alice has to send a single message to Bob such that Bob can find an (approximate) maximum matching of the whole graph G. We specifically study the best approximation ratio achievable via protocols where Alice communicates only O~(n) bits to Bob.

There has been a growing interest on the robust communication model due to its connections to the random-order streaming model. An algorithm of Assadi and Behnezhad [ICALP'21] implies a $(2/3 + \varepsilon_0 \sim .667)$ -approximation for a small constant $0 < \varepsilon_0 < 10^{-18}$, which remains the best-known approximation for general graphs. For bipartite graphs, Assadi and Behnezhad [Random'21] improved the approximation to .716 albeit with a computationally inefficient (i.e., exponential time) protocol.

In this paper, we study a natural and efficient protocol implied by a random-order streaming algorithm of Bernstein [ICALP'20] which is based on edge-degree constrained subgraphs (EDCS) [Bernstein and Stein; ICALP'15]. The result of Bernstein immediately implies that this protocol achieves an (almost) (2/3 ~ .666)-approximation in the robust communication model. We present a new analysis, proving that it achieves a much better (almost) (5/6 ~ .833)- approximation. This significantly improves previous approximations both for general and bipartite graphs. We also prove that our analysis of Bernstein's protocol is tight.

Presenter: AZARMEHR, Amir Session Classification: Track A-4