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## Faster parameterized algorithms for modification problems to minor-closed classes

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Abstract: Let calG be a minor-closed graph class and let G be an n-vertex graph. We say that G is a {\emptyset k-apex} of calG if G contains a set S of at most k vertices such that  $G \setminus S$  belongs to calG. Our first result is an algorithm that decides whether G is a k-apex of calG in time  $2^{\mathsf{poly}(k)} \cdot n^2$ .

This algorithm improves the previous one, given by Sau, Stamoulis, and Thilikos [ICALP 2020, TALG 2022], whose running time was  $2^{\text{poly}(k)} \cdot n^3$ . The {\em elimination distance} of G to calG, denoted by  $\text{ed}_{calG}(G)$ , is the minimum number of rounds required to reduce each connected component of G to a graph in calG by removing one vertex from each connected component in each round. Bulian and Dawar [Algorithmica 2017] proved the existence of an {\sf FPT}-algorithm, with parameter k, to decide whether  $\text{ed}_{calG}(G) \leq k$ . This algorithm is based on the computability of the minor-obstructions and its dependence on k is not explicit.

We extend the techniques used in the first algorithm to decide whether  $\operatorname{ed}_{calG}(G) \leq k$  in time  $2^{2^{2^{\operatorname{poly}(k)}}} \cdot n^2$ . This is the first algorithm for this problem with an explicit parametric dependence in k. In the special case where  $\operatorname{cal}G$  excludes some apex-graph as a minor, we give two alternative algorithms, one running in time  $2^{2^{\operatorname{cal}O(k^2\log k)}} \cdot n^2$  and one running in time  $2^{\operatorname{poly}(k)} \cdot n^3$ .

As a stepping stone for these algorithms, we provide an algorithm that decides whether  $\operatorname{ed}_{calG}(G) \leq k$  in time  $2^{calO(\operatorname{tw-}k+\operatorname{tw}\log\operatorname{tw})} \cdot n$ , where tw is the treewidth of G. This algorithm combines the dynamic programming framework of Reidl, Rossmanith, Villaamil, and Sikdar [ICALP 2014] for the particular case where calG contains only the empty graph (i.e., for treedepth) with the representative-based techniques introduced by Baste, Sau, and Thilikos [SODA 2020]. In all the algorithmic complexities above, {\sf poly} is a polynomial function whose degree depends on calG, while the hidden constants also depend on calG.

Finally, we provide explicit upper bounds on the size of the graphs in the minor-obstruction set of the class of graphs  $calE_k(calG) = \{G \mid \operatorname{\sf ed}_{calG}(G) \leq k\}$ .

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