

# Connected k-Center and k-Diameter Clustering

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Lukas Drexler, Jan Eube, Kelin Luo, Heiko Röglin, Melanie Schmidt and Julian Wargalla

**Abstract:** Motivated by an application from geodesy, we study the connected k-center problem and the connected k-diameter problem. These problems arise from the classical k-center and k-diameter problems by adding a side constraint. For the side constraint, we are given an undirected connectivity graph  $G$  on the input points, and a clustering is now only feasible if every cluster induces a connected subgraph in  $G$ . Usually in clustering problems one assumes that the clusters are pairwise disjoint. We study this case but additionally also the case that clusters are allowed to be non-disjoint. This can help to satisfy the connectivity constraints.

Our main result is an  $O(1)$ -approximation algorithm for the disjoint connected k-center and k-diameter problem for Euclidean spaces of low dimension (constant  $d$ ) and for metrics with constant doubling dimension. For general metrics, we get an  $O(\log^2(k))$ -approximation. Our algorithms work by computing a non-disjoint connected clustering first and transforming it into a disjoint connected clustering.

We complement these upper bounds by several upper and lower bounds for variations and special cases of the model.

**Presenter:** LUO, Kelin

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