Contribution ID: 102 Type: not specified

Optimal Decremental Connectivity in Non-Sparse Graphs

Thursday, July 13, 2023 4:00 PM (20 minutes)

Anders Aamand, Adam Karczmarz, Jakub Łącki, Nikos Parotsidis, Peter Rasmussen and Mikkel Thorup

Abstract: We present a dynamic algorithm for maintaining the connected and 2-edge-connected components in an undirected graph subject to edge deletions. The algorithm is Monte-Carlo randomized and processes any sequence of edge deletions in $O(m+n\ poly(\log n))$ total time. Interspersed with the deletions, it can answer queries to whether any two given vertices currently belong to the same (2-edge-)connected component in constant time. Our result is based on a general Monte-Carlo randomized reduction from decremental c-edge-connectivity to a variant of fully-dynamic c-edge-connectivity on a sparse graph.

For non-sparse graphs with $\Omega(n\ poly(\log n))$ edges, our connectivity and 2-edge-connectivity algorithms handle all deletions in optimal linear total time, using existing algorithms for the respective fully-dynamic problems. This improves upon an $O(m\log(n^2/m) + n\ poly(logn))$ -time algorithm of Thorup [J.Alg. 1999], which runs in linear time only for graphs with $\Omega(n^2)$ edges.

Our constant amortized cost for edge deletions in decremental connectivity in non-sparse graphs should be contrasted with an $\Omega(\log n/\log\log n)$ worst-case time lower bound in the decremental setting [Alstrup, Husfeldt, and Rauhe FOCS'98] as well as an $\Omega(\log n)$ amortized time lower-bound in the fully-dynamic setting [Patrascu and Demaine STOC'04].

Presenter: KARCZMARZ, Adam **Session Classification:** Track A-1