## Sample-based distance-approximation for subsequence-freeness

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Abstract: In this work, we study the problem of approximating the distance to subsequence-freeness in the sample-based distribution-free model. For a given subsequence (word)  $w = w_1 \dots w_k$ , a sequence (text)  $T = t_1 \dots t_n$  is said to contain w if there exist indices  $1 \le i_1 < \dots < i_k \le n$  such that  $t_{i_j} = w_j$  for every  $1 \le j \le k$ .

Otherwise, T is w-free. Ron and Rosin (ACM TOCT 2022) showed that the number of samples both necessary and sufficient for one-sided error testing of subsequence-freeness in the sample-based distribution-free model is  $\Theta(k/\epsilon)$ .

Denoting by Dist(T, w, p) the distance of T to w-freeness under a distribution  $p : [n] \to [0, 1]$ , we are interested in obtaining an estimate wDist, such that  $|wDist - Dist(T, w, p)| \le \delta$  with probability at least 2/3, for a given distance parameter  $\delta$ . Our main result is an algorithm whose sample complexity is  $\tilde{O}(k^2/\delta^2)$ . We first present an algorithm that works when the underlying distribution p is uniform, and then show how it can be modified to work for any (unknown) distribution p. We also show that a quadratic dependence on  $1/\delta$  is necessary.

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