

# The Fine-Grained Complexity of Boolean Conjunctive Queries and Sum-Product Problems

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**Abstract:** We study the fine-grained complexity of evaluating Boolean Conjunctive Queries and their generalization to sum-of-product problems over an arbitrary semiring. For these problems, we present a general *semiring-oblivious* reduction from the  $k$ -clique problem to any query structure (hypergraph). Our reduction uses the notion of *embedding* a graph to a hypergraph, first introduced by Marx~\cite{Marx13}. As a consequence of our reduction, we can show tight conditional lower bounds for many classes of hypergraphs, including cycles, Loomis-Whitney joins, some bipartite graphs, and chordal graphs. These lower bounds have a dependence on what we call the *clique embedding power* of a hypergraph  $H$ , which we believe is a quantity of independent interest. We show that the clique embedding power is always less than the submodular width of the hypergraph, and present a decidable algorithm for computing it. We conclude with many open problems for future research.

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