

A dichotomy for succinct representations of homomorphisms

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Abstract: The task of computing homomorphisms between two finite relational structures A and B is a well-studied question with numerous applications. Since the set $\text{Hom}(A,B)$ of all homomorphisms may be very large having a method of representing it in a succinct way, especially one which enables us to perform efficient enumeration and counting, could be extremely useful.

One simple yet powerful way of doing so is to decompose $\text{Hom}(A,B)$ using union and Cartesian product. Such data structures, called d -representations, have been introduced by Olteanu and Zavodny in the context of database theory. Their results also imply that if the treewidth of the left-hand side structure A is bounded, then a d -representation of polynomial size can be found in polynomial time. We show that for structures of bounded arity this is optimal: if the treewidth is unbounded then there are instances where the size of any d -representation is superpolynomial. Along the way we develop tools for proving lower bounds on the size of d -representations, in particular we define a notion of reduction suitable for this context and prove an almost tight lower bound on the size of d -representations of all k -cliques in a graph.

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